

Sets and Relations

Question1

Let S be a non-empty subset of \mathbb{R} . Consider the following statement:

p : There is a rational number $x \in S$ such that $x > 0$.

Which of the following statements is the negation of the statement p ?

MHT CET 2024 (16 May Shift 1)

Options:

- A. There is a rational number $x \in S$ such that $x \leq 0$.
- B. There is no rational number $x \in S$ such that $x \leq 0$.
- C. Every rational number $x \in S$ satisfies $x \leq 0$.
- D. $x \in S$ and $x \leq 0 \Rightarrow x$ is not a rational number.

Answer: C

Solution:

Given statement is

$\exists x \in S$, such that $x > 0$

$\therefore \sim (\exists x \in S, \text{ such that } x > 0)$

$\equiv \forall x \in S, x \leq 0$

i.e., Every rational number $x \in S$ satisfies $x \leq 0$.

Question2

If $n(A) = 4, n(B) = 2$. Then the number of subsets of the set $A \times B$ each having at least 3 elements are MHT CET 2024 (15 May Shift 1)

Options:

- A. 275
- B. 510
- C. 219
- D. 256

Answer: C



Solution:

$$n(A) = 4, n(B) = 2$$

$$\therefore n(A \times B) = 4 \times 2 = 8$$

$$\text{Required numbers} = {}^8C_3 + {}^8C_4 + \dots + {}^8C_8$$

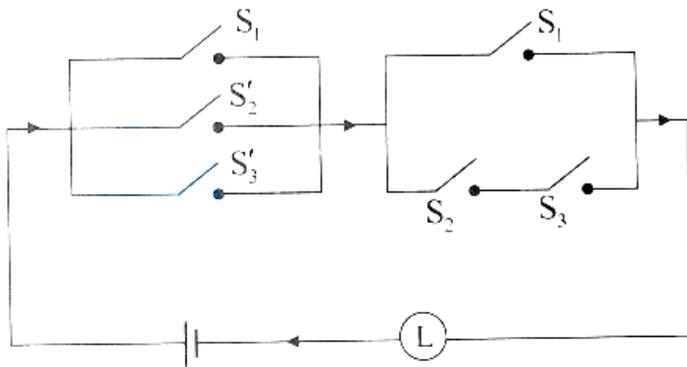
$$= 2^8 - ({}^8C_0 + {}^8C_1 + {}^8C_2)$$

$$= 256 - 37$$

$$= 219$$

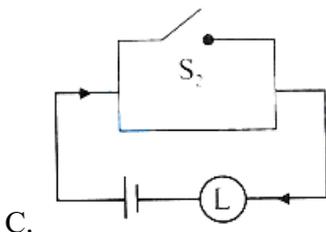
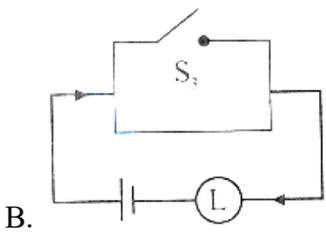
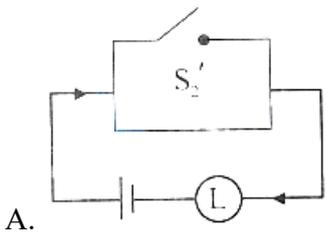
Question3

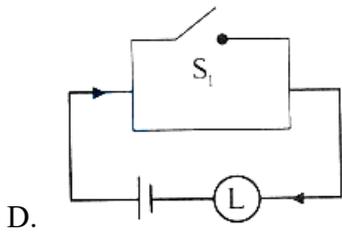
The given circuit is equivalent to



MHT CET 2023 (10 May Shift 1)

Options:





Answer: D

Solution:

The symbolic form of the given circuit is

$$(p \vee \sim q \vee \sim r) \wedge (p \vee (q \wedge r))$$

$$\equiv p \vee [(\sim q \vee \sim r) \wedge (q \wedge r)]$$

...[Distributive law]

$$\equiv p \vee [\sim (q \wedge r) \wedge (q \wedge r)]$$

...[De Morgan's law]

$$\equiv p \vee F$$

...[Complement law]

$$\equiv p$$

[Identity law]

Question4

Let $A = [a, b, c, d]$, $B = [1, 2, 3]$. **Relation R_1, R_2, R_4 are as follows:**

$$R_1 = [(a, 1), (b, 2), (c, 1), (d, 2)]$$

$$R_2 = [(a, 1), (b, 1), (c, 1), (d, 1)]$$

$$R_3 = [(a, 2), (b, 3), (c, 2), (d, 2)]$$

$$R_4 = [(a, 1), (b, 2), (a, 2), (d, 3)], \text{ then}$$

MHT CET 2021 (20 Sep Shift 2)

Options:

- A. only R_3 and R_4 are not functions
- B. only R_1 and R_2 are not functions
- C. only R_3 is not a function
- D. only R_4 is not a function

Answer: D

Solution:

We find that in R_4 , $f(a) = 1$ and $f(a) = 2$. Hence R_4 is not a function.

Question5

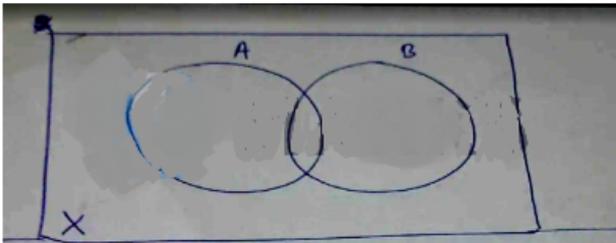
If A and B are subsets of universal set X such that $n(X) = 200$, $n(A) = 90$, $n(B) = 80$, $n(A' \cap B') = 40$, then $n(A \cap B) =$
MHT CET 2020 (20 Oct Shift 2)

Options:

- A. 70
- B. 80
- C. 20
- D. 10

Answer: B

Solution:



$$\begin{aligned}n(A \cap B') &= n(A) - n(A \cap B) \\n(x) &= 200 \\n(A \cap B) &= n(A) + n(B) + 2(A' \cap B') \\&\quad - n(X) \\n(A \cap B) &= 90 - 10 \\&= 80\end{aligned}$$

Question6

If $A = \{x, y, z\}$, $B = \{1, 2\}$, then the total number of relations from set A to set B are
MHT CET 2020 (16 Oct Shift 1)

Options:

- A. 64
- B. 16



C. 32

D. 8

Answer: A

Solution:

It is given that $A = \{x, y, z\}$ and $B = \{1, 2\}$.

$$\therefore A \times B = \{(x, 1), (x, 2), (y, 1), (y, 2), (z, 1), (z, 2)\}$$

Since $n(A \times B) = 6$, the number of subsets of $A \times B$ is 2^6 .

Therefore, the number of relations from A to B is 2^6 .

Question 7

Given $A = \{1, 2, 3, 4, 5\}$, $B = \{1, 4, 5\}$. If R is a relation from A to B such that $(x, y) \in R$ with $x > y$, then range of R is MHT CET 2020 (14 Oct Shift 2)

Options:

A. $\{1, 4\}$

B. $\{4, 5\}$

C. $\{1, 4, 5\}$

D. $\{2, 4\}$

Answer: A

Solution:

$$A = \{1, 2, 3, 4, 5\}; B = \{1, 4, 5\}$$

$$R: A \rightarrow B(x > y)$$

Domain

$$\begin{pmatrix} 2 \\ 3 \\ 4 \\ 5 \end{pmatrix}$$

Range

$$\begin{pmatrix} 1 \\ 4 \end{pmatrix}$$

$$\text{Range } R = \{1, 4\}$$

Question8

If $A = \{x/x \text{ is a prime number, } 0 \leq x \leq 9\}$, then the number of elements of powerset of A is MHT CET 2020 (13 Oct Shift 2)

Options:

- A. 12
- B. 4
- C. 16
- D. 8

Answer: C

Solution:

$$A = \{2, 3, 5, 7\}$$

$$\begin{aligned} \text{Power set of } A &= 2^4 \\ &= 16. \end{aligned}$$

Question9

If $A = \{2, 4\}$, $B = \{3, 4, 5\}$, then $(A \cap B) \times (A \cup B) =$ MHT CET 2020 (12 Oct Shift 1)

Options:

- A. $\{(3, 2), (3, 4), (4, 4), (5, 4)\}$
- B. $\{(2, 3), (2, 4), (2, 5)\}$
- C. $\{(4, 2), (4, 3), (4, 4), (4, 5)\}$
- D. $\{(4, 3), (4, 4), (4, 5)\}$

Answer: C

Solution:



$$A \cap B = \{4\}$$

$$A \cup B = \{2, 3, 4, 5\}$$

Hence

$$(A \cap B) \times (A \cup B) \\ = \{(4, 2), (4, 3), (4, 4), (4, 5)\}$$

Question10

If $A = \{x \in R : x^2 - 5|x| + 6 = 0\}$, then $n(A) =$ _____ MHT CET 2019 (02 May Shift 1)

Options:

- A. 2
- B. 0
- C. 1
- D. 4

Answer: D

Solution:

$$\text{Given: } A = \{x \in R : x^2 - 5|x| + 6 = 0\}$$

$$x^2 - 5|x| + 6 = 0 \Rightarrow |x|^2 - 5|x| + 6 = 0$$

$$|x| = 2, 3 \Rightarrow x = \pm 2, \pm 3$$

$$\text{Hence, } n(A) = 4$$

Question11

If $A = \{x | x \in N, x \text{ is a prime number less than } 12\}$ and $B = \{x | x \in N, x \text{ is factor of } 10\}$, then $A \cap B = \dots$ MHT CET 2019 (Shift 2)

Options:

- A. $\{2\}$
- B. $\{2, 5\}$
- C. $\{2, 5, 10\}$
- D. $\{1, 2, 5, 10\}$



Answer: B

Solution:

We have, $\{x|x \in N, x|, \text{is a prime number less than } 12\}$

$$= \{2, 3, 5, 7, 11\}$$

And $B = \{x|x \in N, x \text{ is a factor of } 10\} = \{1, 2, 5, 10\}$

$$A \cap B = \{2, 5\}$$

Question 12

If $X = \{4^n - 3n - 1 : n \in N\}$ and $Y = \{9(n - 1) : n \in N\}$, then $X \cap Y =$ **MHT CET 2018**

Options:

A. X

B. Y

C. ϕ

D. $\{0\}$

Answer: A

Solution:

$$X = \{4^n - 3n - 1 : n \in N\}$$

$$X = \{(1 + 3)^n - 3n - 1 : n \in N\}$$

$$X = \left\{ 1 + 3n + \frac{3^2 n(n-1)}{2!} + \frac{3^3 n(n-1)(2n-1)}{6} \dots 3n - 1 \right\}$$

$$X = \left\{ 3^2 (n-1)n \left(\frac{1}{2!} + \frac{3(2n-1)}{6} + \dots \right) \right\}$$

$$X = \left\{ 9(n-1)n \left(\frac{1}{2!} + \dots \right) \right\}$$

$$Y = \{9(n-1) : n \in N\}$$

$$\therefore X \subseteq Y$$

$$\therefore X \cap Y = X$$

(or)

Put $n = 1, 2, 3, 4, 5, 6, \dots$ in X and Y

$$X = \{0, 9, 54, \dots\}$$

$$Y = \{0, 9, 18, 27, 36, 45, 54, 63, \dots\}$$

$$X \subseteq Y$$

$$\therefore X \cap Y = X$$

Question13

The chances to fail in Physics are 20% and the chances to fail in Mathematics are 10%. What are the chances to fail in at least one subject? MHT CET 2008

Options:

- A. 28%
- B. 38%
- C. 72%
- D. 82%

Answer: A

Solution:

Let $P(A) = \frac{20}{100} = \frac{1}{5}$, $P(B) = \frac{10}{100} = \frac{1}{10}$ Since, event are independent and we have to

$$\begin{aligned} P(A \cup B) &= P(A) + P(B) - P(A) \cdot P(B) \\ \text{find} \quad &= \frac{1}{5} + \frac{1}{10} - \frac{1}{5} \cdot \frac{1}{10} \\ &= \frac{3}{10} - \frac{1}{50} = \frac{14}{50} = \frac{14}{50} \times 100 = 28\% \end{aligned}$$

